

$$f(x) = x^3 + k \ln x \quad (k \in \mathbb{R}) \quad f'(x) = 3x^2 + \frac{k}{x}$$

$$k = 6$$

$$y = f(x) \quad (1, f(1))$$

$$g(x) = f(x) - f(x) = \frac{9}{x}$$

$$k = 3$$

$$x_1, x_2 \in [1, \infty) \quad x_1 < x_2$$

$$\frac{f(x_1) - f(x_2)}{2} = \frac{f(x_1) - f(x_2)}{x_1 - x_2}$$

$$y = 9x - 8$$

$$g(x) = 9x - 8 \quad 0, 1 \quad 1,$$

$$g(x) = 9x - 8 \quad g(1) = 1$$

$$f(x) = x^3 + k \ln x \quad f'(x) = 3x^2 + \frac{k}{x}$$

$$x_1, x_2 \in [1, \infty) \quad x_1 < x_2 \quad \frac{x_1}{x_2} = t \quad (t > 1)$$

$$x_1 - x_2 = f(x_1) - f(x_2) = 2 \left( \frac{f(x_1)}{x_1} - \frac{f(x_2)}{x_2} \right)$$

$$x_1 - x_2 = 3x_1^2 \frac{k}{x_1} - 3x_2^2 \frac{k}{x_2} = 2 \left( x_1^3 - x_2^3 + k \ln \frac{x_1}{x_2} \right)$$

$$x_1^3 - x_2^3 - 3x_1^2x_2 - 3x_1x_2^2 - k \frac{x_1}{x_2} - \frac{x_2}{x_1} - 2k \ln \frac{x_1}{x_2}$$

$$x_2^3 - t^3 - 3t^2 - 3t - 1 - k - t - \frac{1}{t} - 2 \ln t$$

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$$\frac{3x_1^2 \frac{k}{x_1} 3x_2^2 \frac{k}{x_2}}{2} \frac{x_1^3 x_2^3 k \ln \frac{x_1}{x_2}}{x_1 x_2}$$

$$\frac{3}{2} x_1^2 x_2^2 \frac{k}{2} \frac{x_1 x_2}{x_1 x_2} x_1^2 + x_1 x_2 + x_2^2 + k \frac{\ln x_1}{x_1} \frac{\ln x_2}{x_2}$$

$$x_1 x_2^3 k \frac{x_1^2 x_2^2}{x_1 x_2} 2k \ln \frac{x_1}{x_2}$$

$$t x_1 x_2 1 g t t x_2^3 k \frac{1}{x_2} t x_2 \frac{1}{t} 2k \ln t 2k \ln x_2$$

$$g' t 3 t x_2^2 k \frac{1}{x_2} x_2 \frac{1}{t^2} \frac{2k}{t} 3 t x_2^2 k \frac{t x_2^2}{x_2 t^2} \frac{t x_2^2 3t^2 x_2 k}{x_2 t^2} 0$$

$$g t x_2, g t g x_2 0$$

$$x_1 x_2^3 k \frac{x_1^2 x_2^2}{x_1 x_2} 2k \ln \frac{x_1}{x_2}$$

$$t x_1 t g t g x_2 0$$

$$g t g x_2$$

$$x_1 x_2^3 k \frac{x_1^2 x_2^2}{x_1 x_2} 2k \ln \frac{x_1}{x_2}$$

$$\frac{x_1}{x_2} x_1 x_2 \frac{x_1 x_2}{x_2} \frac{x_1}{x_2} 1$$

$$\frac{x_1}{x_2} 1^3 k \frac{x_1}{x_2} \frac{x_2}{x_1} 2k \ln \frac{x_1}{x_2} 0$$

$$t \frac{x_1}{x_2} 1 h t t 1^3 k(t \frac{1}{t}) 2k \ln t$$

$$h' t 3 t 1^2 k(1 \frac{1}{t^2}) k \frac{2}{t} \frac{t 1^2 3t^2 k}{t^2} 0$$

$$h t 1, h t h 1 0$$

$$x_1 x_2^3 k \frac{x_1^2 x_2^2}{x_1 x_2} 2k \ln \frac{x_1}{x_2}$$

$$\frac{x_1}{x_2} x_1 x_2 \frac{x_1}{x_2} 1$$

$$\frac{x_1}{x_2} = 1 + k \frac{x_1}{x_2} - \frac{x_2}{x_1} - 2k \ln \frac{x_1}{x_2} = 0$$

$$f(x) = e^{mx} - x^2 - mx$$

$$f(x) = (x, 0) \quad (0, )$$

$$x_1, x_2 \in [1, 1] \quad |f(x_1) - f(x_2)| = e - 1 - m$$

$$f(x) = (x - 2)e^x - a(x - 1)^2$$

$a$

$$x_1, x_2 \in f(x)$$

$$x_1, x_2 \in 2$$